## INDIAN SCHOOL SALALAH

## ANNUAL EXAMINATION, MARCH, 2017-18

MAX.MARKS: 80

## CLASS: IX

## MATHEMATICS

TIME: 3 HOURS

## General Instructions:

i. All Questions are compulsory.
ii. The question paper consists of thirty questions divided into 4 sections A, B, C and D.
iii. Section A comprises of 6 questions of 1 mark each, section $B$ comprises of 6 questions of 2 marks each, section C comprises of ten questions of 3 marks each and section D comprises of 8 questions of 4 marks each.
iv. There is no overall choice. However, an internal choice has been provided in four questions of 3 marks each, three questions of 4 marks each. You have to attempt only one of the alternatives in all such questions.
$v$. Use of calculators is not permitted.

## Section-A

1. Find the value of $\frac{1}{2 \sqrt{5}}$ when $\sqrt{5}=2.236$.
2. If $\left(x^{2}+k x-3\right)=(x-3)(x+1)$, then find $k$.
3. One of the angles of a triangle is $65^{\circ}$. Find the remaining two angles, if their difference is $25^{\circ}$.
4. If O is centre of circle as shown in the figure, find $\angle C B D$.
5. If the height and the radius of a cone is tripled, then find the
 ratio of volume of new cone and that of original cone.
6. In a class of 12 students, 5 are boys and the rest are girls. Find the probability that a student selected will be a girl?

## Section-B

7. If $x+y=12$ and $x y=27$, find the value of $x^{3}+y^{3}$.
8. Answer the following:
(i) A point lies on y-axis, and then which coordinate is zero? And what is the representation?
(ii) If a point is at a distance of 2 units from $y$-axis and 3 units from $x$-axis. Write the coordinates.
9. Without plotting the given points on a graph paper, indicate the quadrants in which they lie if
(i) Ordinate $=6$, abscissa $=-3$
(ii) Ordinate $=-6$, abscissa $=4$
(iii) Abscissa $=-5$, ordinate $=-7$
(iv) Ordinate $=3$, abscissa $=5$
10. In the figure, $P Q \perp P R, P Q / / R L, \angle R Q T=38^{\circ}$ and $\angle Q T L=75^{\circ}$, find x and y.

11. A rectangular sheet of paper $44 \mathrm{~cm} \times 20 \mathrm{~cm}$ is rolled along its length and a cylinder is formed. Find the volume of the cylinder.
12. The mean of 16 numbers is 8 . If 2 is added to every number, what will be the new mean?

## Section-C

13. Arrange the following numbers in ascending order: $\sqrt[3]{5}, \sqrt[4]{8}, \sqrt{3}$.
(Or)
Represent $\sqrt{7.3}$ on the number line.
14. Evaluate using suitable identity: $(104)^{3}$
15. If $x=5-2 \sqrt{6}$, then find the value of $x^{2}+\frac{1}{x^{2}}$

## (Or)

If $a+b=c$, then show that $b^{2}+a c=c^{2}-a b$.
16. In the figure, $A C=B D$ prove that $A B=C D$.

17. In the figure, POQ is a line. Ray OR is perpendicular to line PQ . OS is another ray lying between rays OP and OR. Prove that $\angle R O S=\frac{1}{2}(\angle Q O S-\angle P O S)$.

(Or)

In the given figure, $\mathrm{BA} / / \mathrm{ED}$. Prove that $\angle A B C+\angle B C D=180^{\circ}+\angle C D E$.

18. ABCD is a rhombus and $\mathrm{P}, \mathrm{Q}, \mathrm{R}$ and S are mid-points of the sides $\mathrm{AB}, \mathrm{BC}, \mathrm{CD}$ and DA respectively. Show that the quadrilateral $P Q R S$ is a rectangle.
19. ABCD is trapezium with $A B / / D C$. A line parallel to $A C$ intersects $A B$ at $X$ and $B C$ at Y. Prove that $\operatorname{ar}(A D X)=\operatorname{ar}(A C Y)$.
20. The perimeter of a triangle is 50 cm . One side of a triangle is 4 cm longer than the smaller side and the third side is 6 cm less than twice the smaller side. Find the area of the triangle.
21. A hemispherical bowl with radius 6 cm is filled with water. If the water is transferred into cylindrical vessel of base 3 cm , find the height to which the water rises in the cylindrical vessel. [use $\pi=\frac{22}{7}$ ]

## (Or)

A patient in a hospital is given soup daily in a cylindrical bowl of diameter 7 cm . If the bowl is filled with soup to a height of 4 cm , how much soup the hospital has to prepare daily to serve 250 patients? [Use $\pi=\frac{22}{7}$ ]
22. On one page of a telephone directory, there are 200 phone numbers. The frequency distribution of their digits is given below:

| Unit digit | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 19 | 22 | 23 | 19 | 21 | 24 | 23 | 18 | 16 | 15 |

One of the numbers is chosen at random from the page. What is the probability that the unit digit of the chosen number is
(i) less than 3 ?
(ii) more than 7 ?
(iii) between 2 and 5?

## Section-D

23. Find the values of $a$ and $b$ if $a+b \sqrt{6}=\frac{5+\sqrt{6}}{5-\sqrt{6}}$.
24. The polynomials $x^{3}+2 x^{2}-5 a x-8$ and $x^{3}+a x^{2}-12 x-6$ when divided by $x-2$ and $x-3$ leave the remainders are q and p respectively. If $q-p=10$, find the value of $a$ (Or)
If $x+y+z=10, \quad x y+y z+z x=-15$ and $x y z=-12$, then find the values of $x^{2}+y^{2}+z^{2}$ and $x^{3}+y^{3}+z^{3}$.
25. Draw the graph of the equation $7 x+5 y=35$. Find the area of the figure formed by this line and the two axis.

## (Or)

An auto rickshaw fare in the city is charged Rs. 10 for the first kilometer and Rs. 4 per kilometer for subsequent distance covered. Write the linear equation to express the above statement. Draw the graph of the linear equation.
26. ABCD is a parallelogram, if the two diagonals are equal, find the measure of $\angle A B C$.
27. If two equal chords of a circle intersect within the circle, prove that the segments of one chord are equal to corresponding segments of the other chord.

## (Or)

If non-parallel sides of a trapezium are equal, prove that it is cyclic.
28. Construct a triangle ABC , in which $\angle B=60^{\circ}, \angle C=45^{\circ}$ and $\mathrm{AB}+\mathrm{BC}+\mathrm{CA}=11 \mathrm{~cm}$.
29. The residents of a society decided to paint the wall of a cancer detection centre in their premises. If the floor of the cuboidal hall has perimeter equal to 260 m and height 6 m , then
(i) Find the cost of painting the wall (including doors etc.) at the rate of Rs. 9 per $\mathrm{m}^{2}$.
(ii) What is the amount contributed by each one if there are 50 people?
(iii) Which value is depicted by the residents?
30. Draw a histogram and frequency polygon for the following data.

| Cost of Living Index | Number of Months |
| :---: | :---: |
| $440-460$ | 2 |
| $460-480$ | 4 |
| $480-500$ | 3 |
| $500-520$ | 5 |
| $520-540$ | 3 |
| $540-560$ | 2 |
| $560-580$ | 1 |
| $580-600$ | 4 |
| Total | 24 |

